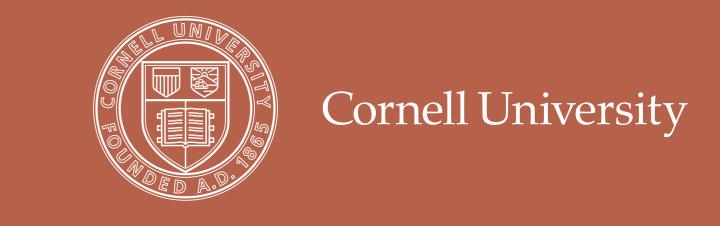
# Stable Coactive Learning via Perturbation

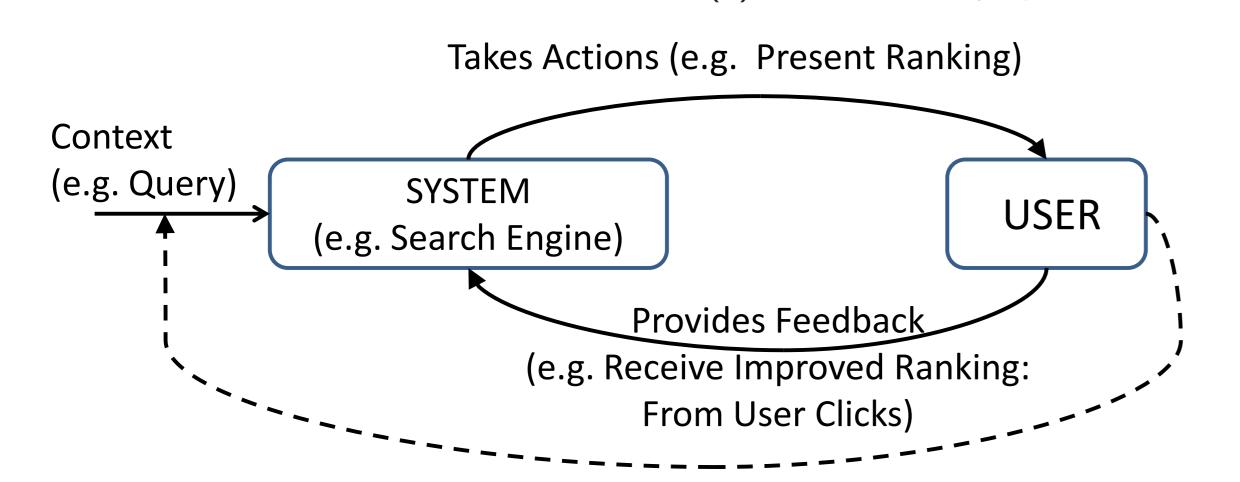
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## **Coactive Learning**

# Coactive Learning: [Shivaswamy and Joachims, 2012]

- $\triangleright$  Given context x, predict object y to optimize utility U(x, y).
- ► Models the interaction between user(s) and learning system.



**Example:** Using implicit feedback for ranking:



## Instability of the Preference Perceptron

# Linear Utility: $U(x, y) = w_*^\top \phi(x, y)$

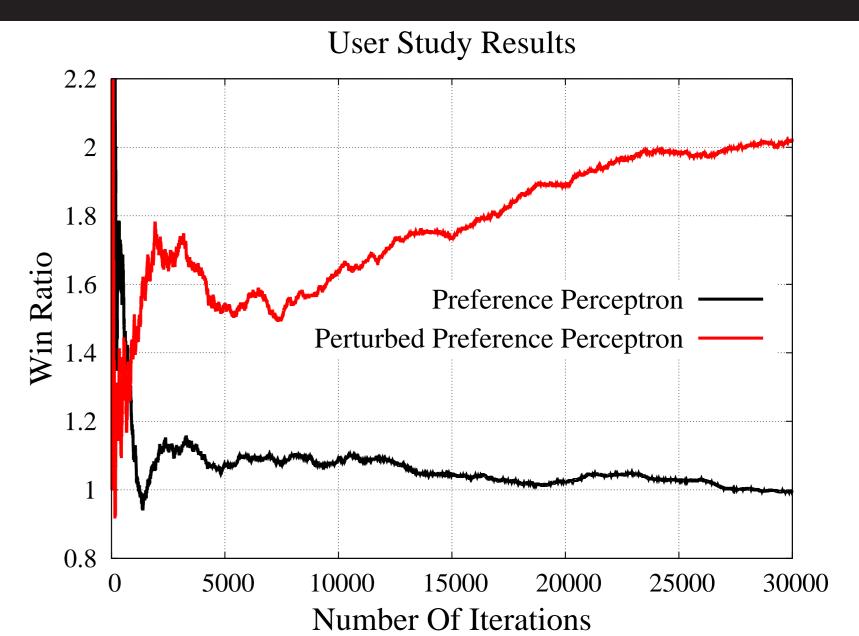
#### Preference Perceptron Algorithm:

(Proposed in [Shivaswamy and Joachims, 2012])

- 1. Initialize weight vector  $\mathbf{w_1} \leftarrow \mathbf{0}$ .
- 2. Given context  $x_t$  present  $\mathbf{y_t} \leftarrow \operatorname{argmax}_{\mathbf{v}} \mathbf{w}_{\mathbf{t}}^{\top} \phi(\mathbf{x_t}, \mathbf{y}).$
- 3. Move clicked documents to top to get feedback ranking  $\bar{\mathbf{y}}_{\mathbf{t}}$ .
- 4.  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + \phi(\mathbf{x}_t, \bar{\mathbf{y}}_t) \phi(\mathbf{x}_t, \mathbf{y}_t)$ .
- 5. Repeat from step 2.

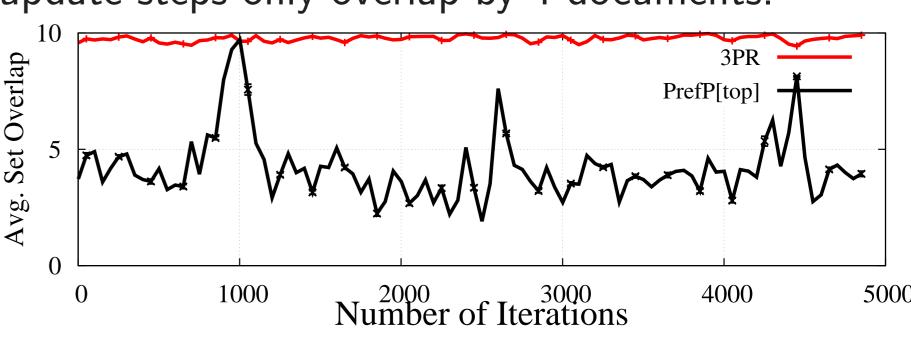
## **User Study:**

- Experimented using live full-text search engine at arxiv.org.
- ► Goal: Learning a ranking function from implicit feedback i.e., user clicks.
- Interleaved evaluation against hand-tuned baseline ranker.
- ► Win ratio of 1 indicates being no better than the baseline. Higher win ratio is better.



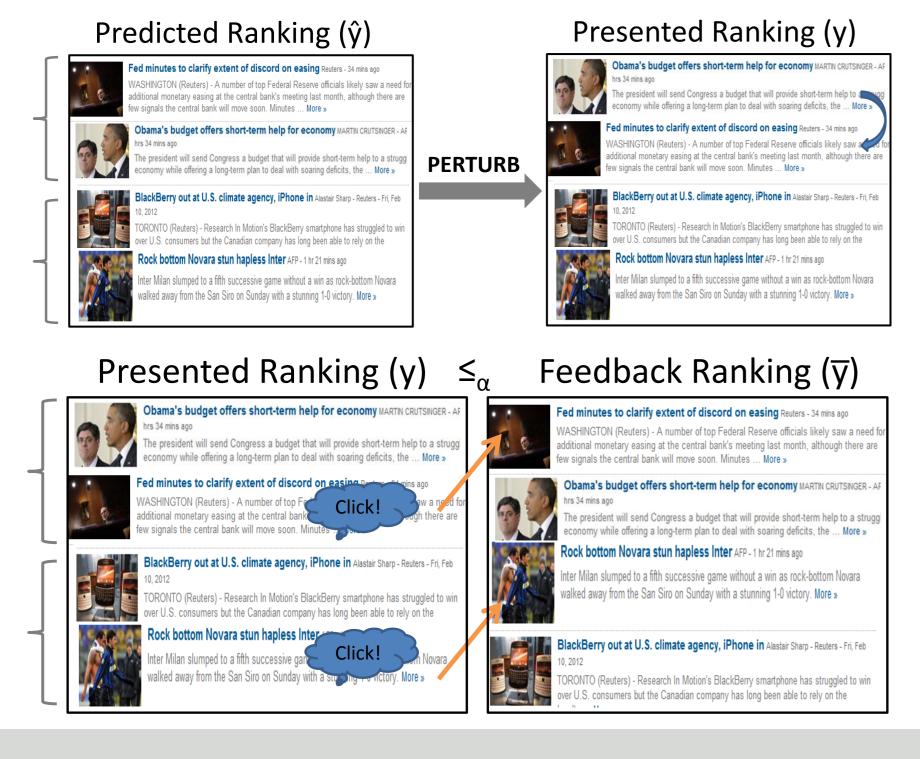
# Preference Perceptron is unstable:

The rankings learned by PrefP never stabilize: Even after thousands of updates, the top 10 documents of the same query before and after 100 update steps only overlap by 4 documents.



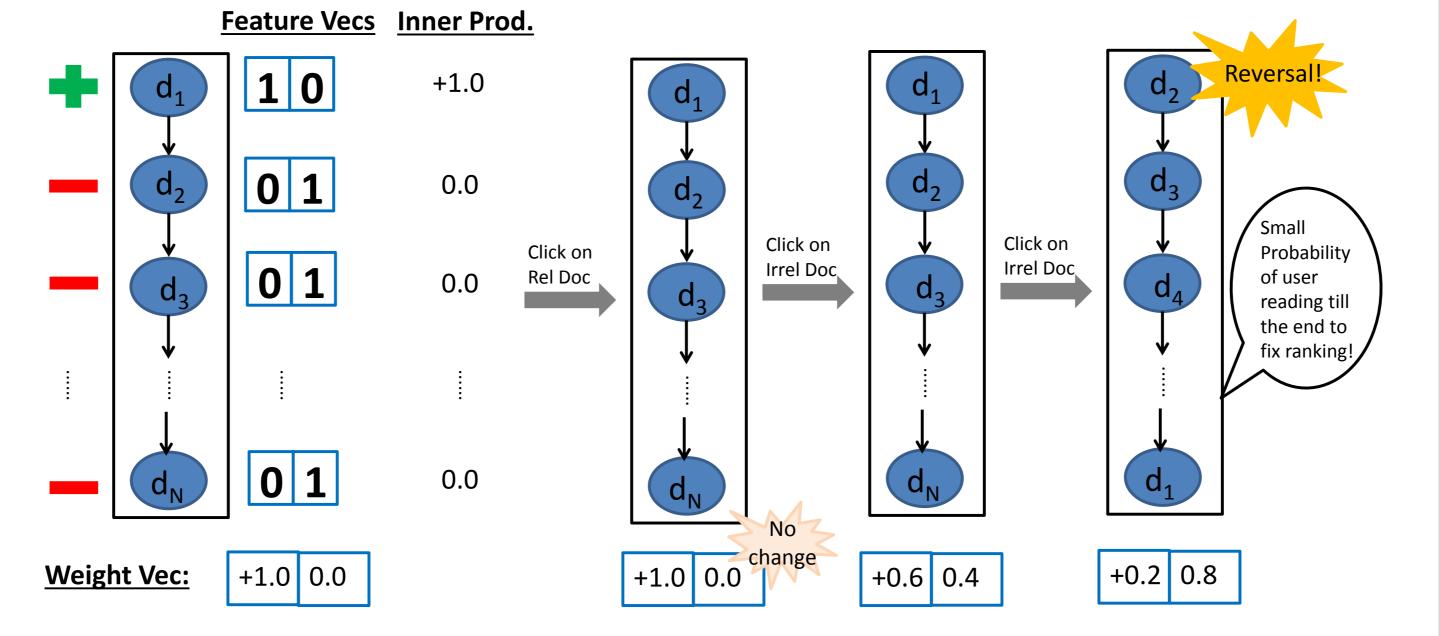
## Perturbed Preference Perceptron

- 1. Initialize weight vector  $\mathbf{w_1} \leftarrow \mathbf{0}$ .
- 2. Given context  $x_t$  predict  $\hat{\mathbf{y}}_{t} \leftarrow \operatorname{argmax}_{\mathbf{v}} \mathbf{w}_{t}^{\top} \phi(\mathbf{x}_{t}, \mathbf{y}).$
- 3. Present  $y_t$ : Obtained by randomly swapping adjacent pairs in  $\hat{\mathbf{y}}_{t}$  with probability  $\mathbf{p}_{t}$ .
- 4. Observe clicks. If clicked document is lower element of pair, move it up by one to get  $\bar{y}_t$ .
- 5.  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + \phi(\mathbf{x}_t, \bar{\mathbf{y}}_t) \phi(\mathbf{x}_t, \mathbf{y}_t)$ .
- 6. Repeat from step 2.

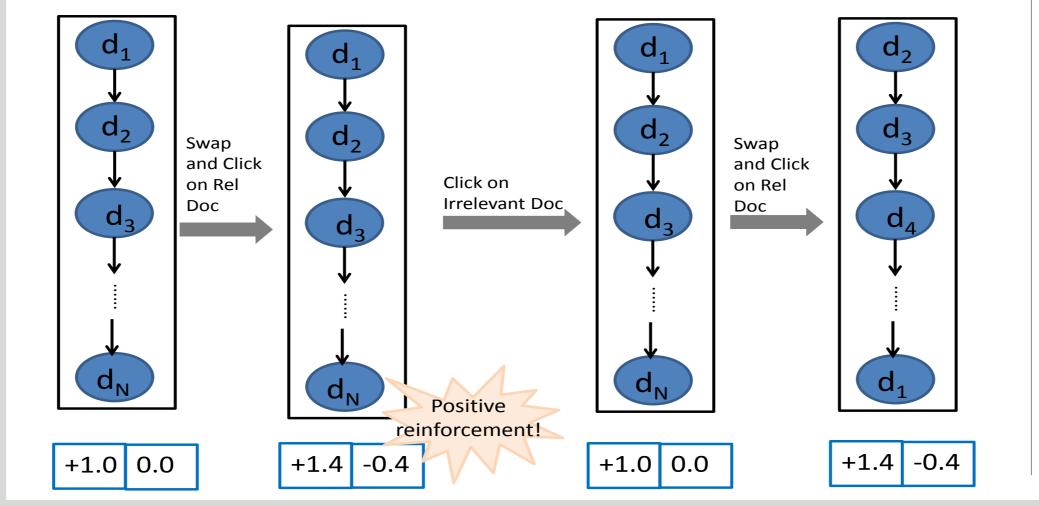


#### Illustrative Example

#### Preference Perceptron (PrefP)



### Perturbed Preference Perceptron (3PR)



For n=10 and 20%user error rate, average rank of the relevant document for 3PR (with p = 0.5) is 2.1 (compared to the 9.4 for PrefP).

# Theoretical Analysis

#### $\alpha$ -Informative Feedback:

We characterize the utility of the feedback received  $\bar{y}_t$  as:

$$E_{\bar{y}}[U(x,\bar{y})] \ge U(x,y) \\
+ \alpha(U(x,y^*) - U(x,y)) - \xi$$

- $\triangleright$  where  $\mathbf{y}^*$  is the optimal and  $\mathbf{y}$ is the presented object.
- ► Note that this is just a characterization (not an assumption).
- Used to prove regret bounds.

#### Regret:

We define the regret after **T** iterations as:

$$\frac{1}{T} \sum_{t=1}^{T} (U(x_t, y_t^*) - E[U(x_t, y_t)]).$$

#### Fixed Probability 3PR

#### The regret of **3PR** with *fixed* swap probability **p** (i.e. $\forall t : p_t = p)$ is:

$$\leq \frac{\sum_{\mathsf{t}=1}^{\mathsf{T}} \xi_{\mathsf{t}}}{\alpha \mathsf{T}} + \frac{\mathsf{p}(1 - \frac{\gamma_2}{\gamma_1}) \mathsf{R} || \mathsf{w}_* ||}{\alpha} \\ + \frac{\sqrt{2(4 - \mathsf{p}^2(1 - \frac{\gamma_2}{\gamma_1})^2) \mathsf{R} || \mathsf{w}_* ||}}{\alpha \sqrt{\mathsf{T}}}.$$

## Dynamic 3PR

For any  $\Delta > 0$ , dynamically setting the swap prob  $p_t$  of 3PRhas regret:

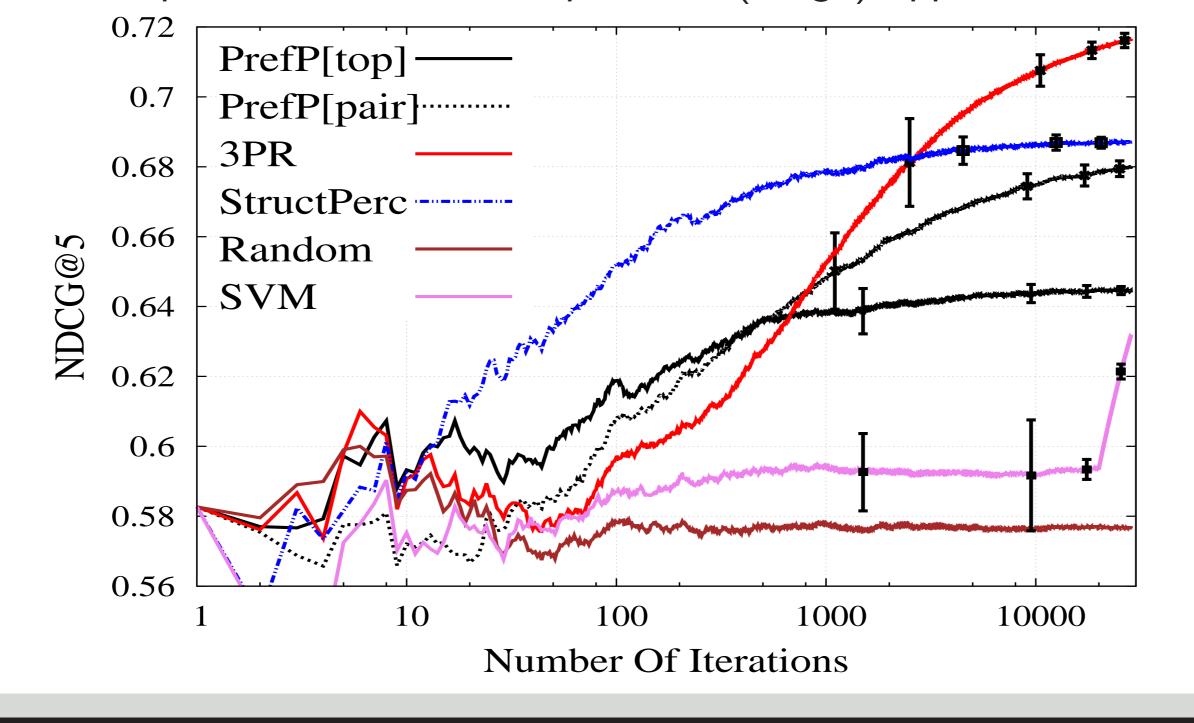
$$\leq \frac{1}{\alpha \mathsf{T}} \sum_{t=1}^{\mathsf{T}} \xi_t + \frac{\|\mathsf{w}_*\|}{\alpha \sqrt{\mathsf{T}}} \times \sqrt{4\mathsf{R}^2 + 2\Delta + 2\mathsf{R}} \sqrt{\frac{4\mathsf{R}^2 + 2\Delta}{\mathsf{T}}}.$$

#### **Experimental Results**

- Performed offline experiments on a search dataset (Yahoo! LTR) and two news recommendation datasets: RCV1 and News.
- Simulated user behavior with and without noise.
- ► NDCG@5 was the utility for all three datasets.

#### Comparison with other methods:

- ► PrefP[top]: Preference Perceptron with move-to-top feedback.
- ▶ PrefP[pair]: PrefP with pairwise feedback *i.e.*, 3PR with  $\mathbf{p_t} = \mathbf{0}$ .
- ► SVM: Ranking SVM with move-to-top feedback.
- Perceptron which receives optimal is (rough) upper bound.



► Small loss in performance due to perturbation, but large gain overall (as seen from PrefP[pair] comparison).

> Websearch RCV1 News Presented y .717  $\pm$  .002 .286  $\pm$  .028 .386  $\pm$  .035 Predicted  $\hat{\mathbf{y}}$  | .723  $\pm$  .002 | .291  $\pm$  .028 | .397  $\pm$  .035

Dynamically setting the swap probability does best:

